- 1 —1. A method for simulating fluid flow within a mold cavity, the method comprising
- 2 the steps of:
- 3 (a) providing a surface representation for a three-dimensional volume
- 4 associated with a mold cavity;
- 5 (b) separating the surface representation into at least a first portion and a
- 6 second portion, the first portion of the surface representation being associated with at
- 7 least one section of the volume having at least one of (i) a substantially invariant
- 8 thickness and (ii) a gradually varying thickness along a length thereof;
- 9 (c) discretizing a first portion of a solution domain bound on an exterior
- thereof by the first portion of the surface representation;
- 11 (d) discretizing a second portion of the solution domain bound on an exterior
- thereof by the second portion of the surface representation;
- (e) defining a plurality of interface elements for the solution domain that
- 14 connect at least part of the first portion of the solution domain to at least part of the
- second portion of the solution domain;
- 16 (f) obtaining values of at least one process variable for the first portion of the
- solution domain using a first set of governing equations; and
- 18 (g) obtaining values of the at least one process variable for the second portion
- of the solution domain using a second set of governing equations.
- 1 2. The method according to claim 1, wherein step (b) is performed automatically.
- 1 3. The method according to claim 2, wherein at least one of step (c), step (d), and
- 2 step (e) is performed automatically.

- 1 4. The method according to claim 2, wherein at least two of step (c), step (d), and
- 2 step (e) are performed automatically.
- 1 5. The method according to claim 1, wherein the surface representation is a surface
- 2 mesh.
- 1 6. The method according to claim 1, wherein the volume represents a molded object.
- 7. The method according to claim 1, wherein the volume represents a mold cavity.
- 1 8. The method according to claim 1, wherein the first set of governing equations in
- step (f), the second set of governing equations in step (g), and a set of interface element
- 3 equations are solved simultaneously, subject to initial conditions and boundary
- 4 conditions.
- 1 9. The method of claim 8, wherein the interface element equations link a portion of
- 2 the solution domain described by governing equations in two spatial dimensions to a
- 3 portion of the solution domain described by governing equations in three spatial
- 4 dimensions.
- 1 10. The method according to claim 1, wherein the at least one process variable is
- 2 selected from the group consisting of temperature, pressure, fluid velocity, stress, and
- 3 fluid flow front position.
- 1 11. The method according to claim 1, wherein there are at least two process variables
- 2 selected from the group consisting of temperature, pressure, fluid velocity, stress, and
- 3 fluid flow front position.
- 1 12. The method according to claim 1, wherein there are at least three process
- 2 variables including temperature, pressure, and fluid velocity.

- 1 13. The method according to claim 1, wherein the method simulates fluid injection in
- 2 the three-dimensional volume.
- 1 14. The method according to claim 13, wherein the method further comprises
- 2 determining a location of at least one injection point.
- 1 15. The method according to claim 1, wherein step (a) comprises providing the
- 2 surface representation from CAD system output.
- 1 16. The method according to claim 15, wherein the CAD system output is in
- 2 stereolithography format or IGES format.
- 1 17. The method according to claim 15, wherein the CAD system output defines a
- 2 surface mesh comprising polygonal elements.
- 1 18. The method according to claim 17, wherein the polygonal elements are triangular
- 2 elements or quadrilateral elements.
- 1 19. The method according to claim 15, wherein the CAD system output defines a
- 2 three-dimensional mesh.
- 1 20. The method according to claim 19, wherein the surface representation is provided
- 2 from a lattice of polygons that bound the three-dimensional mesh.
- 1 21. The method according to claim 15, wherein step (a) comprises using the CAD
- 2 system output as a preliminary mesh and remeshing the preliminary mesh to provide the
- 3 surface representation.
- 1 22. The method according to claim 1, wherein step (a) comprises providing a surface
- 2 representation comprising a mesh of polygonal surface elements.
- 1 23. The method according to claim 22, wherein step (b) comprises defining two or
- 2 more subsurfaces, each subsurface comprising at least one of the surface elements.

- 1 24. The method according to claim 23, wherein step (b) comprises determining
- 2 element properties and nodal properties for each of the surface elements.
- 1 25. The method according to claim 24, wherein step (b) comprises using at least a
- 2 subset of the element properties and nodal properties to classify each of the two or more
- 3 subsurfaces according to curvature.
- 1 26. The method according to claim 23, wherein step (b) comprises defining at least
- 2 one surface loop, each comprising a connected subset of edges of the surface
- 3 representation.
- 1 27. The method according to claim 23, wherein step (b) comprises remeshing at least
- a subset of the two or more subsurfaces using a bisection algorithm.
- 1 28. The method according to claim 23, wherein step (b) comprises determining which
- 2 of the two or more subsurfaces are matched subsurfaces.
- 1 29. The method according to claim 28, wherein each pair of matched subsurfaces is
- 2 separated by a definable thickness.
- 1 30. The method according to claim 28, wherein the first portion of the surface
- 2 representation comprises at least a subset of the matched subsurfaces.
- 1 31. The method according to claim 23, wherein step (b) comprises determining which
- of the two or more subsurfaces are unmatched subsurfaces.
- 1 32. The method according to claim 31, wherein the second portion of the surface
- 2 representation comprises at least a subset of the unmatched subsurfaces.
- 1 33. The method according to claim 23, wherein step (b) comprises determining which
- 2 of the two or more subsurfaces are edge subsurfaces.

- 1 34. The method according to claim 28, wherein step (c) comprises projecting at least
- 2 one of the surface elements from one subsurface in a substantially perpendicular direction
- onto a matched subsurface thereof, thereby defining paired surface elements.
- 1 35. The method according to claim 34, wherein step (c) comprises converting the
- 2 paired surface elements into wedge elements.

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- 1 36. The method according to claim 1, wherein step (c) comprises automatically
- 2 discretizing the first portion of the solution domain.
- 1 37. The method according to claim 1, wherein discretizing in step (c) comprises using
- 2 the first portion of the surface representation to define the first portion of the solution
- 3 domain.
- 1 38. The method according to claim 1, wherein step (c) comprises discretizing the first
- 2 portion of the solution domain using wedge elements.
- 1 39. The method according to claim 38, wherein at least one of the wedge elements
- 2 comprises at least one solution grid point along a thickness thereof.
- 1 40. The method according to claim 38, wherein at least one of the wedge elements is
- 2 a discretely layered element or a continuously layered element.
- 1 41. The method according to claim 1, wherein step (d) comprises automatically
- 2 discretizing the second portion of the solution domain.
- 1 42. The method according to claim 1, wherein step (c) comprises discretizing the first
- 2 portion of the solution domain using hexahedral elements.
- 1 43. The method according to claim 1, wherein step (c) comprises discretizing the first
- 2 portion of the solution domain using shell elements.

- 1 44. The method according to claim 1, wherein step (d) comprises discretizing the
- 2 second portion of the solution domain using polyhedral elements.
- 1 45. The method according to claim 44, wherein the polyhedral elements are
- 2 tetrahedral elements or hexahedral elements.
- 1 46. The method according to claim 1, wherein step (e) comprises defining a set of line
- 2 interface elements.
- 1 47. The method according to claim 46, wherein each of the line interface elements is
- 2 located along an interface of the first portion of the solution domain and the second
- 3 portion of the solution domain.
- 1 48. The method according to claim 46, wherein each of the line interface elements
- 2 comprises at least two nodes of a wedge element of the first portion of the solution
- 3 domain.
- 1 49. The method according to claim 48, wherein each of the line interface elements
- 2 further comprises at least one solution grid point between two of the at least two nodes.
- 1 50. The method according to claim 1, wherein step (e) comprises defining a set of
- 2 planar interface elements.
- 1 51. The method according to claim 1, wherein step (c) is initiated before step (e).
- 1 52. The method according to claim 1, wherein step (e) is initiated before step (d).
- 1 53. The method according to claim 1, wherein the first set of governing equations
- 2 describes fluid flow in two spatial dimensions.

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- 1 54. The method according to claim 1, wherein the first set of governing equations
- 2 describes fluid flow in two spatial dimensions and time.

- 1 55. The method according to claim 1, wherein the first set of governing equations
- 2 describes fluid flow in one spatial dimension and time.
- 1 56. The method according to claim 1, wherein step (f) comprises using a Hele-Shaw
- 2 approximation.
- 1 57. The method according to claim 1, wherein step (g) comprises solving a Navier
- 2 Stokes equation.
- 1 58. The method according to claim 1, wherein step (g) comprises solving a simplified
- 2 Stokes equation.
- 1 59. The method according to claim 1, wherein the second set of governing equations
- 2 comprises conservation of mass, conservation of momentum, and conservation of energy
- 3 equations.
- 1 60. The method according to claim 1, wherein at least one of step (f) and step (g)
- 2 comprises using a meshless scheme.
- 1 61. The method according to claim 60, wherein the meshless scheme is a boundary
- 2 element method, natural element method, or smooth particle hydrodynamics method.
- 1 62. The method according to claim 1, further comprising the step of:
- 2 (h) displaying the values of the at least one process variable directly on a 3D
- 3 representation of the volume.
- 1 63. The method according to claim 1, wherein step (g) comprises using a Mini
- 2 element formulation.
- 1 64. A method for simulating fluid flow within a mold cavity, the method comprising
- 2 the steps of:

- 3 (a) providing a surface representation for a three-dimensional volume
- 4 associated with a mold cavity;
- 5 (b) automatically separating the surface representation into at least a first 6 portion and a second portion;
- 7 (c) defining a solution domain for the three-dimensional volume, where the
- 8 solution domain comprises a first part corresponding to the first portion of the surface
- 9 representation and a second part corresponding to the second portion of the surface
- 10 representation;
- 11 (d) solving for a process variable in the first part of the solution domain; and
- 12 (e) solving for the process variable in the second part of the solution domain.
- 1 65. The method according to claim 64, wherein the first portion of the surface
- 2 representation in step (b) is associated with at least one section of the volume that has at
- least one of (i) a substantially invariant thickness and (ii) a gradually varying thickness
- 4 along a length thereof.
- 1 66. The method according to claim 64, wherein step (c) comprises automatically
- 2 discretizing the first part and the second part of the solution domain.
- 1 67. The method according to claim 64, further comprising the step of defining a
- 2 plurality of interface elements that connect the first part of the solution domain to the
- 3 second part of the solution domain.
- 1 68. The method according to claim 64, wherein step (d) comprises using a first set of
- 2 governing equations and step (e) comprises using a second set of governing equations.
- 1 69. The method according to claim 68, wherein the first set of governing equations
- describes 2.5D flow and the second set of governing equations describes 3D flow.

- 70. A method for automatically defining a hybrid solution domain, the method 1 comprising the steps of:
- (a) identifying a plurality of subsurfaces of a volume associated with a mold 3
- cavity using a representation of the surface of the volume; 4
- (b) 5 matching one or more pairs of the plurality of subsurfaces to identify one
- or more matched pairs of subsurfaces and one or more unmatched subsurfaces; and 6
- (c) defining 7

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- (i) 8 a first portion of a hybrid solution domain bound at least in part by one or more of the matched pairs of subsurfaces and 9
- 10 (ii) a second portion of the hybrid solution domain bound at least in part by one or more of the unmatched subsurfaces. 11
- 71. 1 The method according to claim 70, wherein the volume represents a mold cavity.
- 72. 1 The method according to claim 71, further comprising using the hybrid solution
- 2 domain to model a molding process.
- 73. The method according to claim 70, wherein the representation of the surface of 1
- the volume comprises CAD system output. 2
- The method according to claim 70, wherein the first portion of the hybrid solution 74. 1
- domain is amenable to 2.5D flow analysis, and the second portion of the hybrid solution 2
- 3 domain is amendable to 3D flow analysis.
- 1 75. The method according to claim 70, wherein step (b) comprises classifying each of
- the plurality of subsurfaces according to curvature. 2

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- The method according to claim 70, wherein the matched pairs of subsurfaces each 76. 1
- 2 comprise two subsurfaces that are separated by a substantially constant thickness.

- 1 77. The method according to claim 70, wherein the volume represents a molded
- 2 object.
- 1 78. The method according to claim 77, further comprising using the hybrid solution
- 2 domain in determining a structural property of the molded object.
- 1 79. The method according to claim 78, wherein the structural property is warpage.
- 1 80. An apparatus for simulating fluid flow within a mold cavity, the apparatus
- 2 comprising:
- a memory that stores code defining a set of instructions; and
- 4 (b) a processor that executes said instructions thereby to
- 5 (i) separate a surface representation of a three-dimensional volume
- 6 associated with a mold cavity into at least a first portion and a second portion, the first
- 7 portion of the surface representation being associated with at least one section of the
- 8 volume having at least one of (i) a substantially invariant thickness and (ii) a gradually
- 9 varying thickness along a length thereof;
- 10 (ii) discretize a first portion of a solution domain bound on an exterior
- thereof by the first portion of the surface representation;
- 12 (iii) discretize a second portion of the solution domain bound on an
- exterior thereof by the second portion of the surface representation;
- 14 (iv) define a plurality of interface elements for the solution domain that
- 15 connect at least part of the first portion of the solution domain to at least part of the
- second portion of the solution domain;
- (v) obtain values of at least one process variable for the first portion of
- the solution domain using a first set of governing equations; and

- 19 (vi) obtain values of the at least one process variable for the second
- 20 portion of the solution domain using a second set of governing equations.
- 1 81. An apparatus for defining a hybrid solution domain, the apparatus comprising:
- 2 (a) a memory that stores code defining a set of instructions; and
- 3 (b) a processor that executes said instructions thereby to
- 4 (i) identify a plurality of subsurfaces of a volume associated with a
- 5 mold cavity using a representation of the surface of the volume;
- 6 (ii) match one or more pairs of the plurality of subsurfaces to identify
- 7 one or more matched pairs of subsurfaces and one or more unmatched subsurfaces; and
- 8 (iii) define
- 9 (A) a first portion of a hybrid solution domain bound at least in 10 part by one or more of the matched pairs of subsurfaces and
- 11 (B) a second portion of the hybrid solution domain bound at
  12 least in part by one or more of the unmatched subsurfaces.
- 1 82. The method of claim 2, further comprising the step of re-characterizing a subset
- 2 of the second portion of the solution domain as belonging to the first portion according to
- 3 user input.
- 1 83. The method of claim 2, further comprising the step of re-characterizing a subset
- of the first portion of the solution domain as belonging to the second portion according to
- 3 user input.
- 1 84. The method of claim 1, wherein step (b) comprises separating the surface
- 2 representation into a first portion, a second portion, and at least one additional portion.